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The Relationship Existing between the Weight of a Falling Drop and the Diameter of the Tip from which it Falls

DISSERTATION

SUBMITTED IN PARTIAL FULFILMENT OF THE REQUIRE-MENTS FOR THE DEGREE OF DOCTOR OF PHILOSOPHY IN THE FACULTY OF PURE SCIENCE IN COLUMBIA UNIVERSITY IN THE CITY OF NEW YORK.

BY

JESSIE YEREANCE CANN, A.B., A.M.

NEW YORK CITY

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Easton, Pa.: Eschenbach Printing Company. 1911.



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ACKNOWLEDGMENT.

The following investigation was suggested by and carried out under the direction of Professor J. Livingston R. Morgan. The author desires to extend her sincere thanks and appreciation to Professor Morgan for his helpful assistance, advice and encouragement during the course of the work.

J. Y. C.





The Relationship Existing between the Weight of a Falling Drop and the Diameter of the Tip from which it Falls

INTRODUCTION.

Object of the Investigation.

In 1864, Thomas Tate, as the result of his experiments with water, announced the following laws:

- I. Other things being the same, the weight of a drop of liquid (falling from a tube) is proportional to the diameter of the tube in which it is formed.
- II. The weight of the drop is in proportion to the weight which would be raised in a tube with a bore equal to the outer diameter by capillary action.

III. The weight of a drop of liquid, other things being the same, is diminished by an augmentation of temperature.

Tate's experiments were all made with thin-walled glass tubing, varying in diameter from 0.1-0.7 of an inch, the orifice in each case being ground to a "sharp edge, so that the tube at the part in contact with the liquid might be regarded as indefinitely thin." His weights were calculated from the weight of from five to ten drops of liquid, which formed at intervals of forty seconds, and were collected in a weighted beaker.

Tate's law is generally accepted as equivalent to the expression

$$w = 2 \pi r \gamma,$$

where w is the weight of the falling drop, r the radius of the tube on which it forms, and γ is the surface tension of the liquid. This expression is not exactly as Tate intended it to be formulated, for his law simply states a proportionality; so that the expression should be

$$w = 2 \pi r \gamma K,$$

where K is some constant which will transform the proportionality into an equality.

¹ Phil. Mag., 4th Ser., 27, 176 (1864).

It has also been shown by Morgan and Stevenson,¹ Morgan and Higgins² and Morgan and Thomssen³ contrary to the conclusions of all other workers since Tate that the weight of a single drop of a non-associated liquid falling from a definite tip is regulated by the following laws:

I. The quantity $w\left(\frac{M}{d}\right)^{\frac{2}{3}}$ (w= weight of drop in milligrams, M= molecular weight, d= density) is a linear function of the temperature, becoming zero at a point 6° below the observed critical temperature or a fictitious critical temperature. Expressed mathematically we have then (in the form of Ramsay and Shields, for surface tension)

$$w\left(\frac{M}{d}\right)^{\frac{2}{3}} = k(t_c - t - 6)$$

where t_c is the critical temperature (observed or fictitious) and t is the temperature of observation and k a universal constant, defined by the equation

$$k = \frac{w_1 \Big(\frac{M}{d}\Big)^{\frac{2}{3}} - w_2 \Big(\frac{M}{d}\Big)^{\frac{2}{3}}}{t_2 - t_1}$$

although, as has been shown by Morgan,³ it should not be calculated in this way, owing to the multiplication of error, but from $w\left(\frac{\mathbf{M}}{d}\right)^{\frac{3}{d}} = k_{\mathrm{B}}(288.5-t-6)$ for benzene once for all.

II. The temperature coefficient of the function $w\left(\frac{\mathbf{M}}{d}\right)^3$ i. e., the $k_{\scriptscriptstyle \mathrm{B}}$ of the above equation is a universal constant for such liquids, leading, as has been shown by Morgan,³ to the same value of t_c for any one non-associated liquid at all temperatures of observation.

It has further been shown by Morgan that the above laws hold also when applied to the results of Ramsay and Shields of surface tension, thus confirming Tate's second law.

¹ J. A. C. S., **30,** 360–376 (1908).

² Ibid., 30, 1055-68 (1908).

³ *Ibid.*, May, 1911.

The object of this investigation was to establish conclusively the truth of the first of the above laws, $i.\ e.$, to make an exhaustive study of the relationship existing between the weight of a falling drop and the diameter of the tip from which it falls. For this purpose sixteen different tips were employed, varying in size from about 3 mm. to approximately 8 mm. in diameter. Five representative liquids, including that with practically the largest, as well as that with the smallest possible drop volume, were chosen and the relationship between the drop weights, and the different sized tips studied exhaustively.

Apparatus and Method.

The apparatus used in this work is a new and simple form designed by Morgan¹ and especially adapted to the general needs of the investigator in other lines of chemistry. By it the weight of a falling drop of any liquid from any desired tip can be found at various temperatures, up to within a few degrees of the boiling point, with very great accuracy, every possible form of variable error having been foreseen and avoided. As the results of this work show, the method is indeed one of very great accuracy.

In order to exclude any variation in the results due to changing temperature, all measurements were made in a constant temperature bath. This was of the Ostwald gas type with a transparent bath, stirred by a small electric motor. The temperature employed was 27.8° C., the greatest variation recorded being $\pm 0.03^{\circ}$. The thermometer used here was a certified one reading in fiftieths of a degree.

The five representative non-associated liquids were quinoline, pyridine, benzene, ether and carbon tetrachloride. These five liquids were considered the best because of their great differences in density, surface tension and general physical properties (i. e., viscosity, etc.).

The weight of the drop was obtained by finding, first, that of thirty or more drops, in the following manner. The liquid is sucked over from the supply vessel into the capillary

¹ J. A. C. S., March, 1911.

tubing, and allowed to form a drop on the tip. This drop is held at as nearly as possible its maximum size for 5 minutes, so that the vessel may become saturated with the vapor of the liquid used. Next, thirty consecutive drops are allowed to fall each drop falling of its own weight alone, and the time of the entire determination noted. Then the vessel with the vapor and thirty drops is weighed, being wiped with cheesecloth to constant weight. After the apparatus has been set up again, and has assumed the temperature of the bath by remaining in it for a half hour or more, another determination, a "blank" is taken. This time the liquid is sucked over in the same manner as before, the drop being allowed to hang five minutes, but only five consecutive drops are allowed to fall, the sixth drop being held on the tip without falling for the balance of the time consumed by the first determination. In this way the liquid in the weighing vessel in each determination is exposed for the same length of time to the same evaporating influence both for the hanging drop and the liquid which has fallen, so that the total loss is the same in both cases. By subtracting this 5-drop blank from the 30-drop determination, the weight of one drop is obtained, after dividing the difference by 25. Exactly the same method is to be employed with each liquid used.

The densities used were those determined by Morgan and Higgins.

Liquids.

The benzene used in this work was Kahlbaum's special K. The quinoline was distilled frequently, for when it contains water the results are too low, while when allowed to stand it decomposes, becoming thicker and yellow, and giving high results. Because of the "sticky" nature of quinoline great care had to be taken each time between determinations to clean the capillary tube very thoroughly, and then to prevent liquid rising until the first drop was run over, so that no threads of liquid would be spurted over before the drop, and thus cause the weight to be too large. The pyridine used was Kahlbaum's special K, and remained unchanged—pure and colorless—throughout the entire period of work.

It was found in working with pyridine, particularly with the larger tips, that each drop had to be drawn back into the capillary tube, before being allowed to fall, so that each drop would be exactly like the first drop. It was apparent to the eye in these cases that the regular procedure caused the successive drops to grow smaller, and that the liquid did not extend out to the edge of the tip, and hence would give too low a result. The carbon tetrachloride used was from Baker and was redistilled often. Great care had to be taken in making determinations with this liquid, for the drop volume and surface tension are so small that unless the drop is perfectly controlled at the moment of fall the result will be too large. With tips larger than 4.5 mm. this control is extremely difficult, if possible at all on this form of apparatus, and the results obtained are always too high. This perfect control, however, is one of the essential principles of the drop weight method. The ether was from Kahlbaum, and was always redistilled several times before a determination. Without redistillation the results are always found to be too high.

Results.

In Tables I-V are the experimental results obtained with the sixteen tips used for the liquids studied, together with the values of the function $w\left(\frac{M}{d}\right)^{\frac{2}{3}}$, where w is the drop weight and d the density, both at the same temperature, while M is the molecular weight.

4		TABLE	I.—Ben			
	Wt. 30 drops and vessel. Grams.	Av. wt. of 30 drops and vessel. Grams.	Wt. 5 drops and vessel. Grams.	Av. wt. of 5 drops and vessel. Grams.	Av. wt. of 1 drop. Mgs.	$w\left(\frac{\mathbf{M}}{d}\right)^{\frac{2}{3}}$.
3.048	10.3560 10.3561 10.3561	10.35606	9.9222 9.9222	9.9222	17.355	347.51
3.929	11.1960 11.1960 11.1960	11.1960	10.6569 10.6569	10.6569	21.564	431.77

TABLE I .- (Continued). 4.000 10.4067 10.4067 10.40695 9.8587 9.8586 21.934 439.18 10.4073 $4.514 \begin{cases} 10.0359 & 9.4292 \\ 10.0359 & 10.03586 & 9.4291 & 9.42915 & 24.269 & 485.72 \\ 10.0358 & 9.4291 & 9.42915 & 24.269 & 485.72 \end{cases}$ $4.695 \begin{cases} 9.9938 & 9.3626 \\ 9.9938 & 9.3626 \\ 9.9936 & 9.99373 & 9.3626 & 9.3626 & 25.245 & 505.47 \\ 9.9937 & 9.9937 & 9.3626 & 9.3626 & 25.245 & 505.47 \end{cases}$ 4.978 \begin{cases}
10.8887 & 10.2198 \\
10.8887 & 10.88863 & 10.2198 & 10.2198 & 26.753 & 535.67 \\
10.8885 & 10.88863 & 10.2198 & 26.753 & 535.67 \\
\end{cases} (25 drops) 5.306 \begin{cases}
11.2625 & 10.6918 \\
11.2622 & \\
11.2619 & 11.26233 & 10.6918 & 10.6918 & 28.526 & 571.17 \\
11.2627 & \end{cases} $5.501 \begin{cases} 11.2137 & 10.4754 \\ 10.4756 & 10.4755 \\ 11.2137 & 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 10.4755 & 29.528 & 591.23 \\ 11.2137 & 10.4755 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 & 29.528 &$ 5.500 9.7253 8.9873 8.9873 29.532 591.31 9.7260 5.689 9.7554 8.9922 9.7555 9.7554 8.9920 8.9921 30.532 611.33 9.7553 $5.845 \begin{cases} 11.3907 & 10.6067 \\ 11.3905 & 11.39056 & 10.6068 & 10.60683 & 31.349 & 627.70 \\ 11.3905 & 10.6070 & \\ & & & & & & & \\ 11.3815 & & & & & & \\ 11.3816 & 11.38163 & 10.7159 & 10.7159 & 33.287 & 666.48 \\ 11.3818 & & & & & & \\ \end{array}$

TABLE I.—(Continued).

		Tubuu	1. (0000	vivicu).		
	(25 drops)					
	11.5351		10.8287			
	11.5357		0.0			
	11.5357		10.8282			
6 550	11.5357	T 50548	TO 909 F	10 80846	25 251	mom 0a
0.550	11.5352 1	1.53540	10.0205	10.02040	33.331	101.02
	11.5357					
	11.5357 11.5352 11.5357 11.5357 11.5351					
	(25 drops)		0 6870			
	10.4305		9.6872			
6.844	10.4302	0.43023	9.6870	0.6871	37.156	7/3 07
	10.4302 10.4299 10 10.4303	450-5)	J. 55 / -	3730	140.91
,	45 UIUUS1					
	11.4210 11.4207 1 11.4205		10.6057			
7.387	11.4207.1	1.42073	10.6058	10.60575	10.749	815.91
***	11.4205					
	(25 drops)					
	11.4978 11.4980 1 11.4985		10.6215			
7.859	11.4980 1	1 . 4981	10.6215	10.6215	43.83	877.58
	11.4985					
		M	TT 0			

TABLE II.—OUINOLINE.

		IADLE	11.—QUI	OLINE.		
of tip.	and vessel.	Av. wt. of 30 drops and vessel. Grams.	and vessel.	Av. wt. of 5 drops and vessel. Grams.	Av. wt. of 1 drop Mg.	$w\left(\frac{\mathbf{M}}{d}\right)^{\frac{2}{3}}$.
3.048	10.6755 10.6759 10.6756	10.67566	9·9739 9·9743 9·9741	9.9741	28.063	677.48
3.929	10.8235 10.8238 10.8240	10.82376	9·9594 9·9595	9 · 95945	34 · 573	834.62
4.000	10.8021 10.8020 10.8022	10.8021	9.9229 9.9230 9.9230	9.92296	35.165	848.93
4.514	20 drops 10.0749 10.0749 10.0755 10.0755	10.0752	9·4979 9·4979	9 : 4979	38.487	929.11

TABLE II.—(Continued).

	(20 drops	s)		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		
4.978	8 11.4198 11.4196 11.4197	11.4197	10.7825 10.7825	10.7825	42.48	1025.52
5.501	\[\begin{cases} \precise 11.7336 \\ \precise 11.7330 \\ \precise 11.7333 \end{cases} \]	11.7333	10.5604 10.5604	10.5604	46.916	1132.61
5.500	10.2444 10.2443 10.2445	10.2444	9.0713 9.0715 9.0714	9.0714	46.92	1132.71
5.689	10.2932	10.2935	9.0802	9.0800	48.54	1171.00
5.845	11.6891 11.6892 11.6894	11.68923	10.6955 10.6953	10.6954	49.692	1199.61
	(20 drope					
6.550	(20 drops) [11.7617 11.7611 11.7617 11.7618	11.76158	10.9261	10.9261	55.698	1344.62
6.844	(25 drops) { 10.6615 { 10.6605 10.6612	10.66106	9.7894 9.7894	9.7894	58.111	1402.87
7.387	(20 drops) { 11.6620 11.6615 11.6621	11.66186	10.7150 10.7150	10.7150	63.124	1523.90
7.859	(20 drops) [11.7521 11.7517 11.7515	11.75176	10.7372 10.7372	10.7372	67.638	1632.10

TABLE III.—PYRIDINE.

Diameter of tip. Mm.	Crame	and vessel.	Wt. 5 drops and vessel Grams.	and vessel.	Av. wt. of 1 drop Mg.	$w\left(\frac{M}{d}\right)^{\frac{2}{3}}$.
3.048	10.5144	10.51446	9·9470 9·9470	9.9470	22.699	425.42
		10.6369	9.9288 9.9287 9.9289	9.9288	28.324	530.85
		10.76246		10.0422	28.81	539.96
		10.2606	1			
4.978	11.1390 11.1392 11.1392	11.13913	10.2609 10.2605	10.2607	35.137	658.54
		11.1435		10.17445	38.762	726.48
5.500	10.0003 10.0004 10.0003	10.00033	9.0311 9.0312 9.0312	9.03116	38.767	726.57
		10.0384				
5.845	11.6846 11.6840 11.6848	11.68446	10.6545 10.6546	10.65455	41.197	772.11
(25 drops) 11.8020 11.8029 11.8022 11.8020		10.8792	10.87935	46.146	864.88

TABLE III.—(Continued).

7
7
4
5
5
2

TABLE IV.—CARBON TETRACHLORIDE.

	IABI	E 1 V.—C	AKBUN IE	TRACHLO	KIDE.	
Diameter of tip. Mm.	Wt. 30 drops and vessel, a Grams.	Av. wt. of 30 drops and vessel. Grams.	Wt. 5 drops and vessel. Grams.	Av. wt. of 5 drops and vessel. Grams.	Av. wt. of I drop. Mg.	$w\left(\frac{M}{d}\right)^{\frac{2}{3}}$
	10.5284	10.5283		9.9077	15.515	328.97
	$ \begin{cases} 10.5279 \\ 10.3811 \\ 10.3812 \\ 10.3810 \end{cases} $		9.8895 9.8896 9.8894			
	(so drops))				-
4.000	8.5937 8.5930 8.5931	8.59323	7 · 7934 7 · 7932	7 · 7933	19.998	424.03
	8.1205)	7.1108			
4.514	8.1208 8.1203 8.1204	8.1205	7.1108	7.1108	22.438	475.76
4.695	7 · 9593 7 · 9593 7 · 9594 7 · 9593	7 · 95933	7 · 3713 7 · 3710 7 · 3710 7 · 3708	7.37118	23.526	498.83
			7.3718			

4.978 9.5975 8.9710 8.9711 25.066 531.46 9.5978 9.5977 8.9714 8.9711 25.066 531.46 9.5978 9.5978 8.9714 8.9711 25.066 531.46 9.5978 9.5978 9.5978 8.9714 8.9711 25.066 531.46 5.306 11.3661 11.3661 10.6910 10.6910 27.004 572.58 10.8322 10.8321 10.1265 10.1265 28.224 598.45 10.8321 10.1265 10.1265 28.224 598.45 10.8321 10.1265 10.1265 28.224 598.45 10.8321 10.1265 10.1265 28.224 598.45 10.8321 10.3761 10.6089 10.6084 10.60865 30.698 650.90 11.3761 10.6084 10.60865 30.698 650.90 11.3761 10.6084 10.60865 30.698 650.90 10.5084 10.60865 30.698 650.90 10.5084 10.8317 34.672 735.17 6.844 10.6061 10.6061 9.6906 9.6906 36.62 776.47 TABLE V.—Ether. With Grams Grams Grams Grams Grams (50 drops) of \$\frac{1}{2}\$ of \$1						TABLE I	(C	ontinued)_	, server	
4.978 9.5980 9.59775 8.9714 8.9711 25.066 531.46 9.5978 5.306 11.3661 10.6910 10.6910 27.004 572.58 10.8320 10.1265 10.1265 28.224 598.45 10.8321 10.1265 10.1265 28.224 598.45 10.8321 5.500 9.6944 9.69445 8.9871 8.9872 28.29 599.82 5.689 9.7327 9.7327 8.9938 8.9938 29.556 626.69 11.3761 10.6084 10.60865 30.698 650.90 11.3761 10.6084 10.60865 30.698 650.90 6.200 11.5330 11.5330 10.7172 10.7172 32.632 691.91 6.550 11.6985 11.6985 10.8317 10.8317 34.672 735.17 6.844 10.6061 10.6061 9.6906 9.6906 36.62 776.47 TABLE V.—ETHER. TABLE V.—ETHER. Wt. Of a drospot of tip. and vessel. a	,			9.	-5975		8.970	9		
5.306 11.3661 11.3661 10.6910 10.6910 27.004 572.58 5.501 10.8320 10.8321 10.1265 10.1265 28.224 598.45 5.501 9.6945 8.9873 8.9872 28.29 599.82 5.689 9.7327 9.7327 8.9938 8.9938 29.556 626.69 5.845 11.3760 10.6089 10.6084 10.60865 30.698 650.90 6.200 11.5330 11.5330 10.7172 10.7172 32.632 691.91 6.550 11.6985 11.6985 10.8317 10.8317 34.672 735.17 6.844 10.6061 10.6061 9.6906 9.6906 36.62 776.47 TABLE V.—Ether. Wt. Av. wt. Diameter 30 drops of 30 dro			078	9.	5977	0 -077-			25 066	FOX 16
5.306 11.3661 11.3661 10.6910 10.6910 27.004 572.58 5.501 10.8320 10.8321 10.1265 10.1265 28.224 598.45 5.501 9.6945 8.9873 8.9872 28.29 599.82 5.689 9.7327 9.7327 8.9938 8.9938 29.556 626.69 5.845 11.3760 10.6089 10.6084 10.60865 30.698 650.90 6.200 11.5330 11.5330 10.7172 10.7172 32.632 691.91 6.550 11.6985 11.6985 10.8317 10.8317 34.672 735.17 6.844 10.6061 10.6061 9.6906 9.6906 36.62 776.47 TABLE V.—Ether. Wt. Av. wt. Diameter 30 drops of 30 dro		4.	970	9.	. 5900	9.59775	0.9/12	+ 0.9/11	25.000	531.40
5.300 { 11.3661 11.3661 10.6910 10.6910 27.004 572.58 5.501 { 10.8320		4								
5.501 \begin{cases} 10.8322 & 10.8321 & 10.1265 & 10.1265 & 28.224 & 598.45 \\ 10.8321 & 10.8321 & 10.1265 & 10.1265 & 28.224 & 598.45 \\ 5.500 \begin{cases} 9.6945 & 8.9873 & 8.9872 & 28.29 & 599.82 \\ 5.689 & 9.7327 & 9.7327 & 8.9938 & 8.9938 & 29.556 & 626.69 \\ 5.845 \begin{cases} 11.3760 & 10.6089 & 10.6084 & 10.60865 & 30.698 & 650.90 \\ 5.845 \begin{cases} 11.3762 & 11.3761 & 10.6084 & 10.60865 & 30.698 & 650.90 \\ 6.200 & 11.5330 & 11.5330 & 10.7172 & 10.7172 & 32.632 & 691.91 \\ 6.550 & 11.6985 & 11.6985 & 10.8317 & 10.8317 & 34.672 & 735.17 \\ 6.844 & 10.6061 & 10.6061 & 9.6906 & 9.6906 & 36.62 & 776.47 \\ \text{TABLE V.—ETHER.} Wt. Av. wt. of 30 drops of 10.6061 of 30 drops of 10.6084 o		5.	306	II.	3661	11 2661	10.6910)	27 004	570 F8
5.500 { 9.6945				1					4	5/2.50
5.500 { 9.6945				10	.8320	0	10.126	5	0	0
5.500 { 9.6945		5 ·	501	10	8322	10.8321	10.126	5 10.1265	28.224	598.45
5.689 9.7327 9.7327 8.9938 8.9938 29.556 626.69 5.845 \begin{bmatrix} \text{II.3760} & 10.6089 & 10.6084 & 10.60865 & 30.698 & 650.90 \\ 6.200 11.5330 & 11.5330 & 10.7172 & 10.7172 & 32.632 & 691.91 \\ 6.550 & 11.6985 & 11.6985 & 10.8317 & 10.8317 & 34.672 & 735.17 \\ 6.844 & 10.6061 & 10.6061 & 9.6906 & 9.6906 & 36.62 & 776.47 \\ \text{TABLE VETHER.} \\ \text{Wt.} & \text{Av. wt.} & of 30 drops of tip. and vessel. and vessel. and vessel. and vessel. and vessel. Grams. Gr				10.	.0321					
5.689 9.7327 9.7327 8.9938 8.9938 29.556 626.69 5.845 \begin{bmatrix} \text{II.3760} & 10.6089 & 10.6084 & 10.60865 & 30.698 & 650.90 \\ 6.200 11.5330 & 11.5330 & 10.7172 & 10.7172 & 32.632 & 691.91 \\ 6.550 & 11.6985 & 11.6985 & 10.8317 & 10.8317 & 34.672 & 735.17 \\ 6.844 & 10.6061 & 10.6061 & 9.6906 & 9.6906 & 36.62 & 776.47 \\ \text{TABLE VETHER.} \\ \text{Wt.} & \text{Av. wt.} & of 30 drops of tip. and vessel. and vessel. and vessel. and vessel. and vessel. Grams. Gr		5	500	9	6945		8.987	3		
5.845		<i>J</i> .	500	9	.6944	9.69445	8.987	1 8.9872	28.29	599.82
5.845		5.	689	9.	. 7327	9.7327	8.993	8.9938	29.556	626.69
6.200 11.5330 11.5330 10.7172 10.7172 32.632 691.91 6.550 11.6985 11.6985 10.8317 10.8317 34.672 735.17 6.844 10.6061 10.6061 9.6906 9.6906 36.62 776.47 TABLE V.—ETHER. Wt. Av. wt. of 30 drops of tip. and vessel. and vessel. and vessel. and vessel. and vessel. Grams. Grams										
6.200 11.5330 11.5330 10.7172 10.7172 32.632 691.91 6.550 11.6985 11.6985 10.8317 10.8317 34.672 735.17 6.844 10.6061 10.6061 9.6906 9.6906 36.62 776.47 TABLE V.—ETHER. Wt. Av. wt. of 30 drops of tip. and vessel. and vessel. and vessel. and vessel. and vessel. Grams. Grams		_	845	II.	. 3760	11 2761			20, 608	650.00
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TABLE V.—ETHER. Wt. Av. wt. of 30 drops of 30 drops of 30 drops of 10. and vessel. and vessel. and vessel. and vessel. and vessel. Grams. Mg. wt. of 20 drops. Mg. wt. of 3.048 { 7.6045 7.6045 7.2107 7.2109 7.2108 9.843 219.23 8.4134 8.4134 8.4135 (50 drops) (11 drops)		6.	550	ΙI	.6985	11.6985	10.831	7 10.8317	34.672	735.17
TABLE V.—ETHER. Wt. Av. wt. of 30 drops			0			(-(-	0 600	6 0 6006	-6 (-	(
Diameter 30 drops of tip. and vessel. and vessel. Grams. (50 drops) (10 drops) $3.048 \begin{cases} 7.6045 \\ 7.6045 \\ 7.6045 \end{cases} \begin{array}{c} 7.2107 \\ 7.2107 \\ 7.2204 \end{array} \begin{array}{c} 7.2108 \\ 8.4134 \\ 8.4135 \end{array} \begin{array}{c} 9.843 \\ 8.4134 \\ 8.4135 \end{array} \begin{array}{c} 12.284 \\ 273.61 \\ 8.4135 \end{array} \begin{array}{c} 273.61 \\ 8.4135 \\ (50 drops) \end{array} $		6.	844	10	.0001	10.0001	9.690	9.0900	30.02	770.47
Mm. Grams. Grams. Grams. Grams. Grams. Mg. (20 drops) (10 drops) 3.048 7.6045 7.2107 7.2109 7.2108 9.843 219.23 8.7205 8.4134 8.4135 8.7204 8.4135 (50 drops) (11 drops) (11 drops) (20 drops) (20 drop						TABL	е V.—I	ETHER.		
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3.929 8.7205 8.4134 8.4134 12.284 273.61 8.7204 8.4135 (50 drops) (11 drops)			((50	drops					
3.929 8.7205 8.4134 8.4134 12.284 273.61 8.7204 8.4135 (50 drops) (11 drops)		3.	048	7	.6045	7 6045			0 842	210.02
(50 drops) (11 drops)				1	.0045	7.0045	7.210	9 1.2100	9.043	,219.23
(50 drops) (11 drops)				8	. 7205		8.413	4		
(50 drops) (11 drops)		3.	929	8	. 7206	8.7205	8.413	3 8.4134	12.284	273.61
				0	. /204		0.413,)	45.	
4.000 8.2272 7.7400 8.2272 8.2272 8.2279 8.22743 7.7401 7.74003 12.497 278.36 8.2274 7.7400										
4.000 8.2279 8.22743 7.7401 7.74003 12.497 278.36 8.2274 7.7400				8	.2272		7.7400)		
8.2274 7.7400		4	000	8	.2279	8.22743	7.740	7.74003	12.497	278.36
				8	. 2274	. ,0	7.740)		

TABLE V.—(Continued).

` (50 drops) (10 drops)			
4.514	9.1339 9.1344 9.1347 9.1349	9.13448	8.5816 8.5818 8.5820 8.5823 8.5820	8.58194	13.813	307.67
4.695	7.7829 7.7831 7.7830	7.7830	7.4019 7.4019 7.4020	7.40193	15.243	339.51
5.501	7.6328 7.6327 7.6329	7.6328	7.2122 7.2121 7.2122	7.21216	16.825	374.76
5.500	7 · 7575 7 · 7574 7 · 7575	7.75746	7.3367 7.3369 7.3368	7.3368	16.827	374.79
5.689	7·7775 7·7776 7·7775	7 · 77753	7 · 3400 7 · 3400	7.3400	17.501	389.82
5.845	7 · 7895 7 · 7894 7 · 7896	7.7895	7 · 3394 7 · 3393 7 · 3395	7 · 3394	18.004	401.02
6.550	8.9719 8.9720 8.9720	8.97196	8.4555 8.4556 8.4554	8.4555	20.659	460.14
6.844	8.6478 8.6480 8.6479	8.6479	8.1043 8.1045 8.1044	8.1044	21.74	484.23
7.387	8.6256 8.6257 8.6255	8.6256	8.0254 8.0255 8.0253	8.0254	24.008	534 · 75
7.859	8.4755 8.4759 8.4750	8.47546	7.8232 7.8230	7.8231	26.095	581.23

On all three tips below 4.514 mm. benzene, quinoline, pyridine and ether showed drop profiles which were very much larger at the bottom of the drop than at the top or than the diameter of the tip itself, so that on all these tips we should expect the results to be non-concordant when various liquids are compared, for the amount of the bulging, and consequently of the weight of the liquid falling is here independent of the diameter of the tip from which it falls. On the tips from 4.514 up to and including 5.501 the control of the drop was perfect with all the liquids except carbon tetrachloride, and at most the profile of the drop showed that the edges of the lower part are simply a continuation of the edges of the tip and none extends beyond.

Carbon tetrachloride can only be perfectly controlled on tip of 4.514 and on the two sizes below, the drop on all the larger tips spurting at the last moment and carrying down with it an excess of liquid. This is due to the small drop volume, together with the small surface tension of this liquid, which makes the drop at its lower extremity very small, and very liable to break down.

It is to be remembered here that the perfect control is lost only on the form of apparatus in question, for the long capillary burette used by Morgan and Higgins would undoubtedly show perfect control on considerably larger tips, for the long tail of liquid in the narrow capillary only allows a very slow formation of the drop at best.

Ether is found to be difficultly controlled on the 5.689; while only on the larger ones is trouble experienced with benzene, pyridine and quinoline. We should expect then on the tips from 3.929 up to and including 4.514 that carbon tetrachloride would be the criterion for other like liquids, for its drop volume is so small that the edges of the drop never extend beyond lines parallel to the edges of the tip itself.

As soon as perfect control is lost, the drop which falls is too large for it does not fall of its own weight alone, but has projected with it some of the liquid which under perfect control would remain on the tip. This increase in weight continues to increase with the diameter of the tip until the

maximum drop volume has been attained, after which the edges of the drop pull away from the tip; when, provided the control were still perfect, too small a drop for that tip would result. As the control, however, is not perfect, we should expect the value to become too high as control is lost, then to become correct when lack of control is just balanced by the decreasing effect of the drop pulling away from the tip; and finally the drop would probably remain of the same weight on all larger tips. Although the diameters of the above tips were measured on a dividing engine, the mean of a number of determinations on each of three diameters being taken, the accuracy is certainly not much greater than o.o. mm. owing to the fact that the tips were never perfectly circular in section, and in some cases flaws had developed in the edge which made the measurement difficult, although probably it affected the drop weight but slightly.1 In

TABLE VI.

			Values	for—.	
Diameter of tip. Mm.	Benzene. Mg.	Quinoline. Mg.	Pyridine. Mg.	CC4. Mg.	Ether. Mg.
3.048	5.6970	9.2069	7 4470	5.0902	3.2291
3.929	5.4884 5.4835	8.7992 8.7913	7.2089 7.2025	5.0008 4.9995	3.1265 3.1243
4.514	5.3762	8.5260	7.0471	4.9706	3.0601
4.695	5.3769 5.3743	8.5335	7.0585	5.0108	3.0620
5.306	5 · 3752			5.0883	
5.501	5.3677 5.3694	8.5286 8.5309	7.0463 7.0484	5.1307 5.1436	3.0585 3.0593
5.689	5.3668	8.5126	7.0441	5.1952	[3.0763]
5.845	5.3630	8.5009 8.4967	7.0477	5.2516 5.2621	3.0880
6.550	[5.3971]	8.5035	7.0452	5.2934	3.1532
6.844	5.4290 5.5157	8.4908	7.0426 [7.0863]	5.3506	3.1779 3.2498
7.859	5.5766	8.6058	7.1340		3.3201

Table VI are given the values of w/d for each liquid on each tip. From this all those things mentioned above as to the

¹ In this connection it may be said that the 5.501 tip is the one used by Morgan and Thomssen, the results here being slightly lower, due to slight flaws, presumably, which have since developed.

bulging or the loss of control are made clearer than they would be in a small curve, for the difference there would hardly be noticeable.

It will be noted here that from 3.929 to 4.514 the value of w/d for carbon tetrachloride is constant and then increases continually with the size of the tip, showing the effect of lack of control, and later the combination of that with the pulling away of the drop from the edge; while for all the other liquids, on the contrary, up to 4.514 the value decreases then remains constant for a greater or less variation in diameter. The loss of control of ether is first observed on the 5.689 tip, while benzene is lost on the 6.55, and pyridine and quinoline on the 7.387.

TABLE VII.—NORMAL BENZENE CONSTANTS.

		$/M \setminus \frac{2}{3}$
Diameter	$\left(M \right)^{\frac{2}{3}}$	$w\left(\frac{\mathrm{M}}{d}\right)^{\frac{2}{3}}$
of tip. Mm.	$w\left(\frac{\mathrm{M}}{d}\right)^{\frac{2}{3}}$.	$k = \frac{(a)}{288.5 - 27.8 - 6}$
3.048	347.51	1.3644
3.929	431.77	1.6952
4.000	439.18	1.7243
4.514	485.72	1.9078
4.695	505.47	1.9846
4.978	535.67	2.1032
5.306	571.17	2.2425 -
5.501	591.23	2.3213
5.500	591.31	2.3216
5.689	611.33	2.4002
5.845	627.70	2.4645
6.200	666.48	2.6168
6.550	707.82	2.7791
6.844	743.97	2.9210
7.387	815.91	3.2034
7.859	877.58	3.4456

The 4.514 tip is the only one which gives correct results for carbon tetrachloride, for above this tip the results are too high, due to lack of control; while below it, it is impossible to use benzene as the standard because of the bulging of the drop. The carbon tetrachloride k is then the only true one for small tips, and hence in the future will be the liquid used for the standardization of small tips when they are used for

determining the drop weights of liquids similar to that of carbon tetrachloride, i. e., liquids with a very high density and small surface tension. The value of t_c is then to be taken as 283.15° as found on the 4.514 tip, and the normal value of the constant k of the tip calculated from it.

In Table VII are the $k_{\scriptscriptstyle\rm B}$ values found from benzene by use of the formula

$$w\left(\frac{M}{d}\right)^{\frac{2}{3}} = k_B(288.5 - 27.8 - 6)$$

Wherever both benzene and the other liquid give constant results of $\frac{\text{weight}}{\text{diameter}}$ we would expect to find a constant value of k necessary to give the values of t_c as found from the work of Morgan and Higgins by Morgan, on substituting the values of M and d for that liquid in

$$w\left(\frac{\mathbf{M}}{d}\right)^{\frac{2}{3}} = k(t_c - t - 6).$$

These t_c values are 346.6° for pyridine, 521.3° for quinoline, 195° for ether and 283.2° for carbon tetrachloride.

[2.0004.] 2.10 36 2.10 54 2.1066 [2.1311] 4.978 2.1032 [2.2777] 5.307 2.2425 2.32\\$35 2.3\\$230 2.32\\$56 2.32\\$33 2.32\\$30 2.32\\$4 2.40\\$37 2.40\\$12 [2.4\\$8] 5.500 2.3216 [2.3856] [2.3801] 2.3213 5.501 5.689 2.4002

In Table VIII are given those k values for the tips from 4.514-5.501 inclusive, between which we should expect the liquids to be concordant in result, with the exception of carbon tetrachloride, since the values of $\frac{\text{weight}}{\text{diameter}}$ are constant

¹ J. A. C. S., May, 1911.

on them. The value of this latter on the 4.695 tip shows the effect of the lack of perfect control which was noted when the determination was made.

Since, as has been shown by Morgan, surface tension in dynes can be found from drop weight in milligrams by aid of the proportion

$$\gamma:w::K_{\mathbf{B}}:k_{\mathbf{B}},$$

where $K_{\rm B}$ is the value found from Ramsay and Shields very accurate benzene values, calling $t_c=288.5^{\circ}$, *i. e.*, 2.1012; while $k_{\rm B}$ is the similarly determined value for drop weight on the tip in question (see Table VIII).

Table IX contains the values of surface tension in dynes, calculated from drop weight in milligrams by aid of the above relation for the tips considered in Table VIII.

TABLE	IX.—	SURFACE.	TENSIONS.
-------	------	----------	-----------

Diameter of tip.	$k_{\mathrm{B}}.$	Quinoline.	Pyridine.	Ether.	CCI4.
4.514 4.695	1.9078 1.9846	42.39	35.04	15.22	24.71
4.978 5.307	2.1032 2.2425	42.44	35.10	15.23	
5.501	2.3213	42.47	35.09	15.23	-
5.500	2.3216	42.47	35.09	15.23	
5.689	2.4002	42.49	35.08	[15.32]	
	Average,	42.45	35.08	15.23	

TABLE X.—k VALUES.

Diameter of tip.					1
Mm.	Benzene.	Quinoline.	Pyridine.	Ether.	CCI4.
3.048	1.3644	1.3897	1.3601	1.3603	1.3194
3.929	1.6952	1.7121	1.6971	1.6977	1.6722
4.000	1.7243	1.7414	1.7264	I.7272	1.7007
5.689	2.4002	2.4037	2.4012	2.4188	2.4930
5.845	2.4645	2.4608	2.4685	2.4883	2.5893
6.200	2.6168	2.6088			2.7524
6.550	2.7791	2.7582	2.7651	2.8552	2.9245
6.844	2.9210	2.8777	2.8881	3.0046	3.0888
7.387	3.3034	3.1260	3.1368	3.3181	
7.859	3.4456	$3 \cdot 3495$	3.3601	3.6065	

Table X contains the k values and Table XI the γ values calculated similarly for the other tips, which from their $\frac{\text{weight}}{\text{diameter}}$ relations should not be perfectly satisfactory.

It will be noted here that the results are exactly what has already been shown by the simpler w/d ratios, so that we need not discuss them further.

TABLE XI.—SURFACE TENSIONS.

Diameter.		Outratina	Deviation of	T343	0.01
Mm.	Benzene.	Quinoline.	Pyridine.	Ether.	CCI4.
3.048	26.73	43.21	34.96	15.16	23.89
3.929	26.73	42.85	35.10	15.22	24.37
4.000	26.73	42.85	35.11	15.23	24.37
5.689	26.73	42.49	35.08	15.32	25.87
5.845	26.73	42.37	35.12	15.35	26.17
6.200	26.73	42.30			26.20
6.550	26.73	42.11	34.89	15.62	26.21
6.844	26.73	41.80	34.67	15.64	26.34
7.387	26.73	41.40	34 · 34	15.75	
7.859	26.73	41.25	34.20	15.91	

For benzene, using the value of w/d (see Table VI) we find the following relationships (holding for tips from 4.514 to 5.501 inclusive),

$$w = 5.372 \times 2 r$$

and

$$w = 1.710 \times \pi \times 2 r$$

where w is given in milligrams and r in millimeters. The relationship existing between diameter, drop weight and surface tension in dynes per cm. (found from the above, knowing further that $w = \text{constant} \times \gamma$) for any liquid is then

$$w = 0.063972 \times (2 r) \pi \gamma$$
.

Although this relationship was found for benzene it must hold for all the other liquids since the assumption in obtaining it was only that w is proportional to γ .

In Table XII are given the values of γ as calculated from the above equation.

TABLE XII.—SURFACE TENSIONS.

Diameter of tip. Mm.	Benzene.	Quinoline.	Pyridine.	CCI4.	Ether.
4.514	26.75	42.42	35.06	24.73	15.23
4.695	26.75	- 1			
4.978	26.74	42.46	35.12		15.24
5.306	26.75				
5.500	26.72	42.45	35.07		15.22
5.501	26.71	42.44	35.06	*	15.22
5.689	26.70	42.45	35.05		[15.31]
		***************************************		-	
Av.,	. 26 . 73	42.44	35.07	24.73	15.23

Conclusions.

I. The drop weights of benzene, quinoline, pyridine, ether and carbon tetrachloride have been determined at a constant temperature from sixteen different tips varying in size from 3.048 to 7.859 mm. in diameter.

II. All liquids from water, forming practically the largest drop volume to carbon tetrachloride, practically the smallest, follow Tate's law as to proportionality with surface tension on a tip of 4.514 mm. diameter; while, excluding carbon tetrachloride and a few similar liquids with small surface tensions and large densities, the law is found to hold rigidly on tips between 4.514 and 5.501 mm.

III. Smaller tips than 4.514 are adapted only to related liquids when the lower end of the drop bulges in the same way, or those which like carbon tetrachloride form on them normal looking drops similar to those of other liquids on the larger tips.

IV. Tips larger than 5.501 will also hold for similar liquids only, for here it is simply a question of the perfection in the control of the drop.

V. All these things can be observed by closely watching the drop; and a liquid can be said to be satisfactory or not as soon as its drop profile on the tip in question is observed. This is also shown for a series of tips by the values of the

ratios weight diameter.

VI. Surface tensions in dynes per cm. calculated from drop weight in milligrams by multiplication with the ratio of k_{γ}/k_{w} show the same values for the liquids considered when calculated for all tips, the variation being considerably smaller than that from capillary rise by the same observers with different tubes.

VII. It is found that drop weight in milligrams, diameter of the tip in millimeters and surface tension in dynes are related, for tips from 4.514 to 5.501 by the following equation

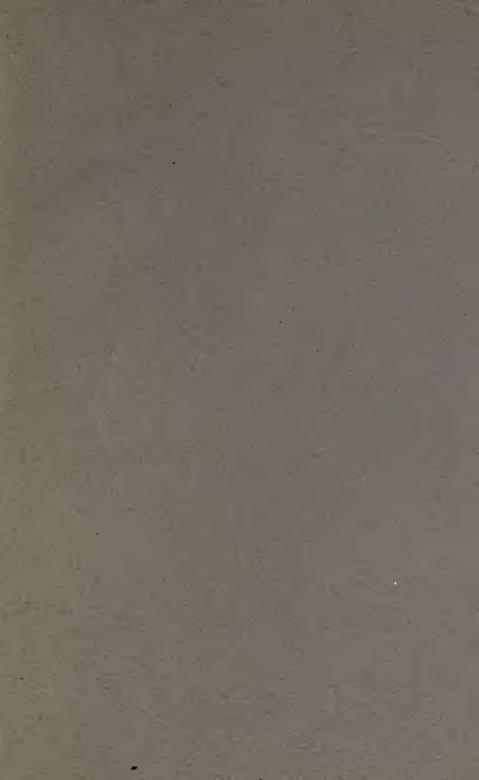
$$w = 0.063972 (2 r) \pi \gamma$$

VIII. It is shown clearly why such a law cannot hold for all liquids on smaller or larger tips than these, but it must be recognized that even on tips beyond these, in either direction, that the results, in terms of surface tension, agree with the others fully as well as do those values determined by aid of capillary rise by various observers.

BIOGRAPHY.

Jessie Vereance Cann was born May 17, 1883, in Newark, New Jersey. In June 1901 she graduated from the Newark High School, and was awarded a four-year scholarship in the Woman's College of Baltimore (Goucher College). She completed her college course in three years, receiving the degree of A.B. in June, 1904. During the years 1904–1909 she taught Science in the Belleville (N. J.) High School. She was a graduate student in Physical Chemistry at Columbia University during the years 1909–1911, as well as during the Summer Sessions of 1907, 1908, 1909 and 1910; and the holder of a Curtis Scholarship 1909–1910, receiving the degree of A.M. in June, 1910.





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